

METROPOLIS: an Applied Dynamic Discrete-Choice Transport Network Model

Fabrice Marchal¹

¹AXONACTIVE AG

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Outline of Part I

1 Motivations

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2 Modelling

- Demand side - departure time choice
- Supply side - linear bottleneck
- Equilibrium
- System optimum
- Day-to-day adjustment process

Outline of Part II (Fabrice Marchal)

3 Design philosophy of METROPOLIS

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- 4 Data issues
 - Demand - static O-D matrices and parameters
 - Network parameters

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 - Convergence properties
 - Peak and off-peak demand

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 - Peak spread measures
 - Capacity expansion
 - Varying levels of demand

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Part I

Dynamic congestion models

Context and motivations

Focus

- Transp. systems
 - Public transport
 - Private modes
 - Car traffic

Context and motivations

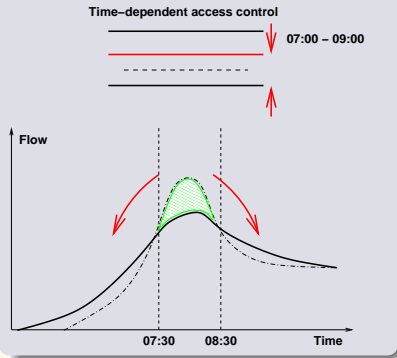
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Reasons for time-dependent models

- Innovative policies

Time-dependent context



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- Technology (ITS)

Time-dependent context



Context and motivations

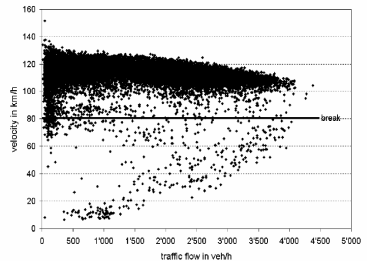
Focus

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Reasons for time-dependent models

- Innovative policies
- Technology (ITS)
- Scientific analysis

Time-dependent context



Travel choices considered

- Mode choice
- Route choice
- **Departure time choice**

Departure time choice - Vickrey's model (1969)

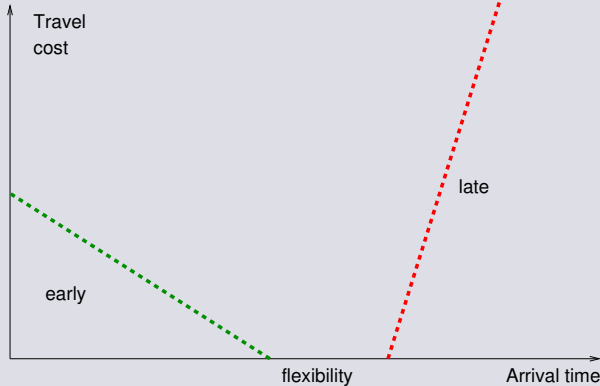
Cost specification:

$$C(t_d) = \alpha\tau(t_d) + \beta \max\{0, t^* - t_a(t_d)\} + \gamma \max\{0, t_a(t_d) - t^*\}$$

- departure time: t_d
- travel time: $\tau(t_d)$
- arrival time: $t_a(t_d) = t_d + \tau(t_d)$
- α : monetary value of time
- β, γ : penalties for early/late arrivals
- t^* : desired arrival time

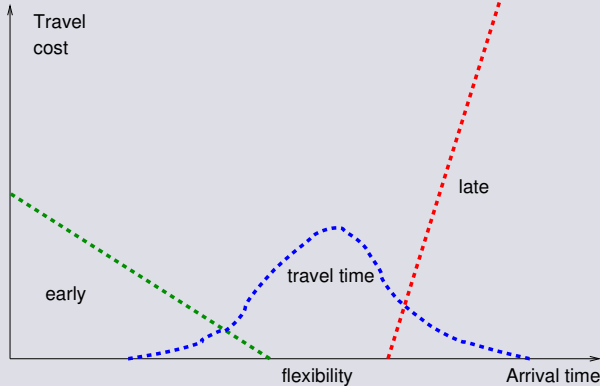
Trade-off between travel time and schedule delay costs

Extension: flexible arrival period



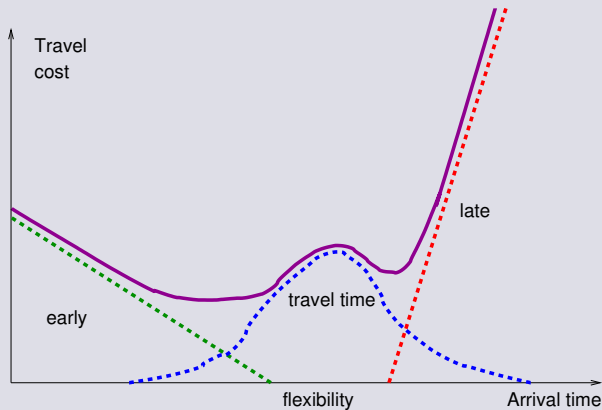
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Typical parameter values

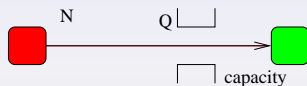
- Linear estimations

	β [\$/h]	γ [\$/h]	t^*	μ [\$]
Com. (Paris/close)	6.0	7.5	N(08:30,60)	2.7
Com. (far suburbs)	8.3	17.4	N(08:24,50)	1.7
Other purposes	5.2	10.6	N(08:54,54)	2.4
			N(10:49,53)	

(value of time from external sources: $\alpha = 13$ \$/h; sources: MADDIF, estimations on Paris area)

- Non-linear estimations

Linear queue for a single O-D pair



Congestion:

$$\tau(t_d) = \frac{Q(t_d)}{\kappa}$$

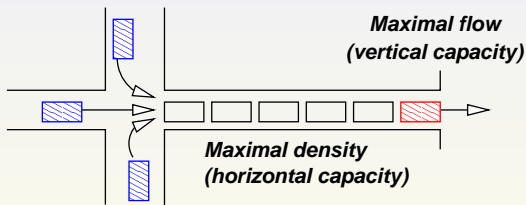
Dynamics:

$$\frac{dQ}{dt} = r(t) - \kappa \text{ if } Q > 0$$

- N : total number of users
- κ : road capacity
- $r(t)$: entry flow

Taking spill-over effects into account

Extension: space limitations and blocking back



Equilibrium - deterministic case

- Cournot-Nash equilibrium condition: $\frac{dC}{dt} = 0$
- individual cost at eq.:

$$C^{eq} = \frac{N}{\kappa} \frac{\beta\gamma}{\beta + \gamma}$$

- departure rate: $r(t) = \kappa \frac{\alpha}{\alpha - \beta}$ (early), $r(t) = \kappa \frac{\alpha}{\alpha + \gamma}$ (late)
- independent of value of time (α)
- schedule delay costs = half of travel cost
- externality = individual cost

System(social) optimum

- condition:

$$r^{so} = \arg \min_{r(t)} C_{TOTAL}$$

$$C_{TOTAL} = \int_{-\infty}^{+\infty} C(t) dt$$

- solution:

$$r^{so}(t) = \kappa \text{ if } t \in T$$

- total cost at sys. optimum:

$$C_{TOTAL}^{so} = \frac{NC^{eq}}{2}$$

Equilibrium and sys. optimum departure rates

Day-to-day adjustment process

Extension: general networks , heterogenous demand

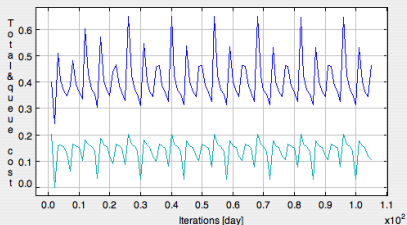
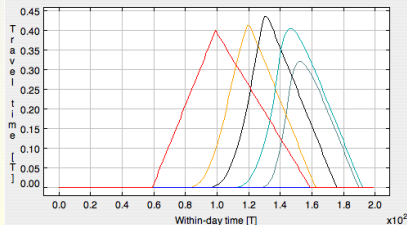
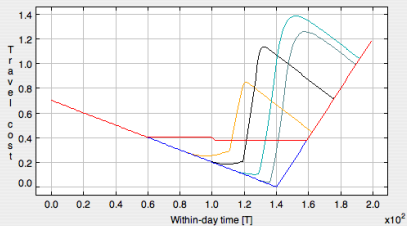
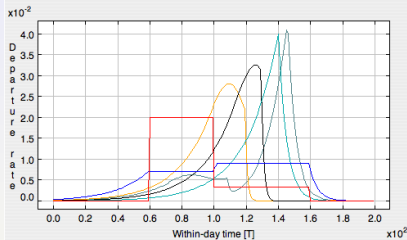
- no closed form available for the equilibrium
- heuristics procedures to adjust decisions **iteratively** (departure/route/mode)
- for instance, inspired by R.U.M.: $U(t_d) = -C(t_d) + \mu\epsilon_{t_d}$

- If ϵ_{t_d} are assumed Gumbel i.i.d \rightarrow logit:

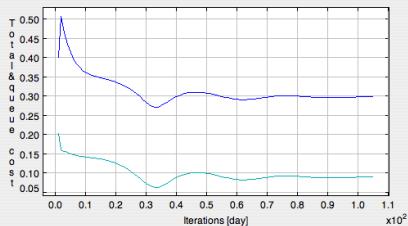
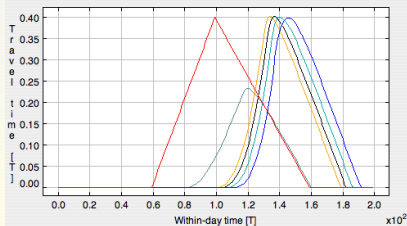
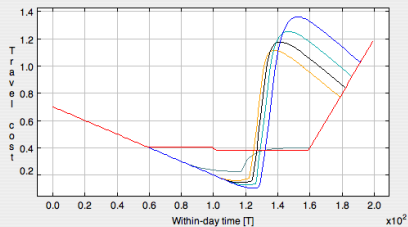
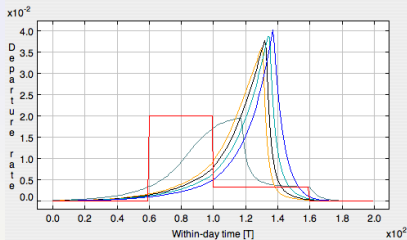
$$\mathcal{P}(t < t_d \leq t + \Delta t) = \frac{\Delta t \exp\left(\frac{-C(t)}{\mu}\right)}{\int_T \exp\left(\frac{-C(u)}{\mu}\right) du}$$

- $\tau_H^{k+1}(t) = \lambda\tau_H^k(t) + (1 - \lambda)\tau_S^k(t)$

Logit adjustment - instabilities - case $\lambda = 0$



Logit adjustment - instabilities - case $\lambda = 0.9$



Part II

METROPOLIS: a tutorial

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Demand

Network

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Convergence

Travel purposes - peak/off-peak

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Road pricing

Peak spread measures

Capacity expansion

Varying level of demand

FAQs

Questions